

3D Graphics Hardware

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Motivation

- VR/AR environment = Hardware setup + VR
 Software Framework + Application
- Detailled knowledge is needed about
 - Hardware: Input Devices & Tracking, Output Devices, 3D Graphics
 - Software: Standards, Toolkits, VR frameworks
 - Human Factors: Usability, Evaluations,
 Psychological Factors (Perception,...)



3D Graphics Hardware - Development

- Incredible development boost of consumer cards in previous ~20 years
- Development driven by game industry
- PC graphics surpassed workstations (~2001)

Consumer Graphics – History

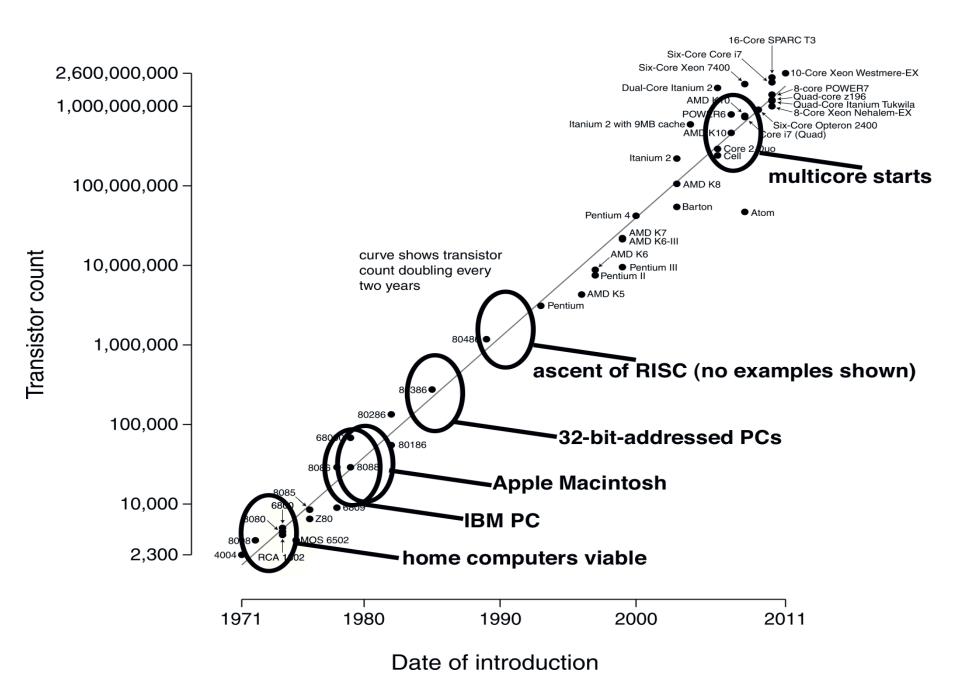
- Up to 1995
 - 2D only (S3, Cirrus Logic, Tseng Labs, Trident)
- 1996 3DFX Vodoo (first real 3D card); Introduction of DX3
- 1997 Triangle rendering (... DX5)
- 1999 Multi-Pipe, Multitexture (...DX7)
- 2000 Transform and lighting (...DX8)
- 2001 Programmable shaders
 - PCs surpass workstations
- 2002 Full floating point
- 2004 Full looping and conditionals
- 2006/07 Geometry/Primitive shaders (DX10, OpenGL 2.1)
- 2007/08 CUDA (Nvidia) GPU General Purpose Computing
- 2009 DX11: Multithreaded rend., Compute shaders, Tessel.
- 2018 Ray-Tracing Cores (RTX) & DirectX Raytracing (in DX12)



Moore's Law

- Gordon Moore, Intel co-founder, 1965
- Exponential growth in number of transistors
- Doubles every 18 months
 - yearly growth: factor 1.6
 - Slow development since 2002 (2.8GHz available since December 2002);
 - But increase in number of cores currently 18-core
 CPUs
- Moore's Law is coming to an end

Microprocessor Transistor Counts 1971-2011 & Moore's Law









NVIDIA Quadro RTX 8000
4608 cores, 576 Tensor cores, 10 GigaRays/sec,
1730 Mhz, 48 GB GDDR6
~15944 GFLOPs (single prec.)

- Faster than the fastest Supercomputer in 2001
- Almost Moore's law squared (^1.5-2.0)
- In the past performance doubled every 9-12 months –
 not anymore but still fast development
- Used in HPC parallel computers (CUDA, Tesla)
 - Molecular dynamics, climate simulations, fluid dynamics
 - ...everything highly parallel computable
- Speedup 10-100x compared to standard processors

And it goes on and on....

- Performance increase expected to continue within the next few years
 - Smaller chip production processes possible (currently 12nm for graphics cards, 10nm CPUs)
 - Multiple graphics cards or GPUs in a PC
 - Multi-core GPUs
- General purpose computing on GPUs
 - OpenCL
 - CUDA / www.gpgpu.org





Mobile ARM Graphics Chips for Smartphones/Tablets

Example: Tegra X1 (2015)

- Processor: 4 ARM Cortex-A57 + 4 A53 cores,
 20nm
- NVIDIA Maxwell 256-core GPU @ 1GHz
 supporting GPU computing CUDA, DirectX
 12, OpenGL 4.5, OpenGL ES 3.1
- Video output 4K x 2K
 @60 Hz, 1080p @120 Hz
- 4k H.265 video decode





What are the benefits in VR/AR?

Which features are needed?



3D Card High End Model

- nVidia Quadro RTX 8000 (~ € 10.000.-)
- 48 GB GDDR6 RAM
- Based on Turing Architecture (Geforce RTX 2080)
- 4608 CUDA cores, 576 Tensor cores
- 672 GB/s Bandwidth
- optimized OpenGL drivers (comp. to consumer card)
- 16K x 16K texture resolution
- DX12, Shader Model 6.1,
 OpenGL 4.6, Vulkan 1.1.78





Some Relevant Features (for VR)

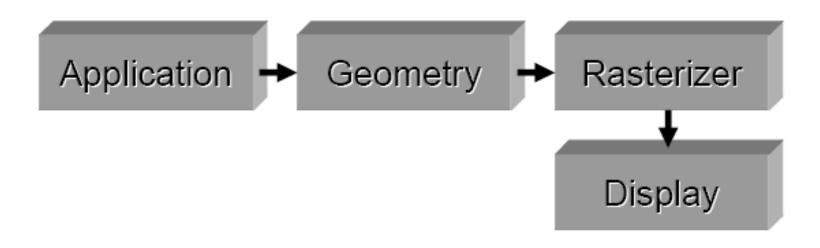
- Memory size: 48 GB
- 4 DisplayPorts 1.4 (8K@60Hz or 4K@120Hz), 1
 VirtualLink (1 connector for VR)
- OpenGL quad-buffered stereo (optional 3-pin sync connector); 3D Vision Pro
- NVLink Technology
- Nvidia Mosaic: 2-8 displays
- Fast 3D Texture transfer; HW 3D Window clipping
- Quadro-Sync (optional) with Framelock and Genlock
- HDR technology, 30-bit color, SDI output option
- Quality: 64 x Full-Scene Antialiasing (FSAA), ...



Explanations & Back to the Basics

3D Graphics Basics

The Graphics Pipeline(s)



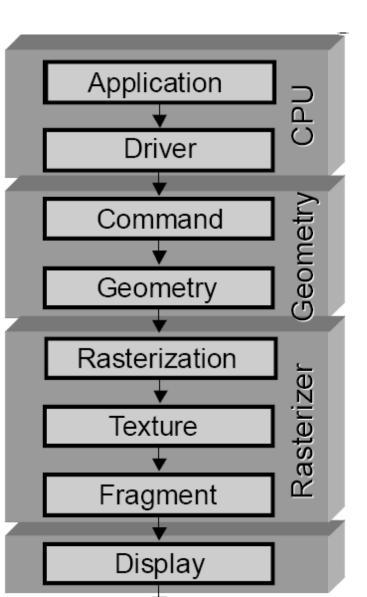


What for ?

Understanding the rendering pipeline is the key to real-time rendering!

- Insights into how things work
 - Understanding algorithms
- Insights into how fast things work
 - Performance

"Historical" Fixed Graphics Pipeline



Purpose: Convert Scene to Pixel Data

Fixed processing of scene

Geometry Stage:

Input: Primitives

Output: 2D window coordinates

Rasterization Stage:

Input: 2D window coordinates

Output: Pixels

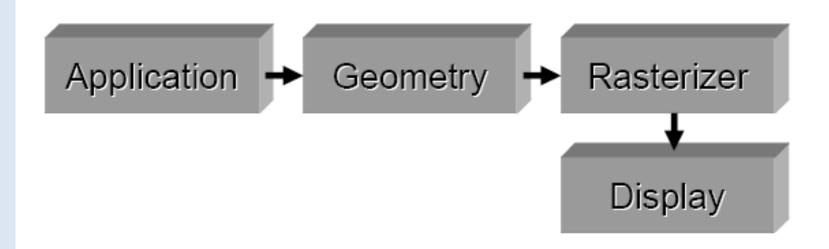
 Fragment: "pixel", but with additional info (alpha, depth, stencil, ...)

Nowadays every part of the pipeline is hardware accelerated!



3D Graphics Basics

The Stages

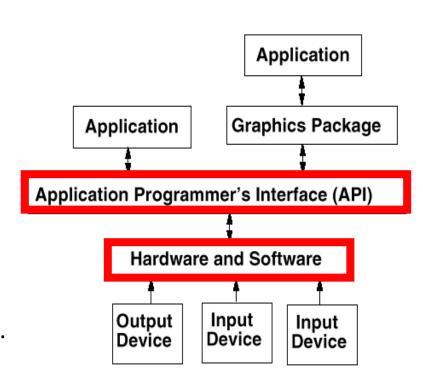




(1) Application Stage:3D Graphics Programming

3D Application Programmer's Interfaces (APIs)

- Access to Hardware
- Standards:
 - OpenGL, Direct3D
- Language: C, C++ (mostly)
- Higher Level APIs based on OpenGL, Direct3D
 - Game Engines
 - Scene Graph APIs:
 - OpenInventor, Java3D
 - OpenSceneGraph, Performer,...



OpenGL – Hello World

```
void init (void) {
#include <GL/glut.h>
                                               glClearColor (0.0, 0.0, 0.0, 0.0);
                                               glMatrixMode(GL_PROJECTION);
void display(void) {
                                               glLoadIdentity();
   glClear (GL COLOR BUFFER BIT);
                                               glOrtho(0.0, 1.0, 0.0, 1.0, -1.0, 1.0);}
   /* draw white polygon (rectangle) with
   corners at (0.25, 0.25, 0.0)
                                           int main(int argc, char** argv)
   and (0.75, 0.75, 0.0) */
   glColor3f (1.0, 1.0, 1.0);
                                               glutInit(&argc, argv);
   glBegin(GL POLYGON);
                                               glutInitDisplayMode (GLUT_SINGLE
   glVertex3f (0.25, 0.25, 0.0);
                                               GLUT_RGB);
   glVertex3f (0.75, 0.25, 0.0);
                                               glutInitWindowSize (250, 250);
   glVertex3f (0.75, 0.75, 0.0);
                                               glutInitWindowPosition (100, 100);
   glVertex3f (0.25, 0.75, 0.0);
                                               glutCreateWindow ("hello");
   glEnd();
                                               init ();
   glFlush ();
                                               glutDisplayFunc(display);
                                               glutMainLoop();
                                               return 0;
  19
```

OpenGL Geometric Primitives



All geometric primitives are specified by vertices

GL POINTS

GL_LINES

....

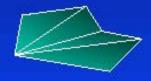
GL LINE STRIP GL LINE LOOP



GL POLYGON



GL TRIANGLES



GL_QUADS



GL TRIANGLE FAN

GL QUAD STRIP

GL TRIANGLE STRIP

16

(1) Application Stage

- Generate database (Scene description)
 - Usually only once
 - Load from disk
 - Build acceleration / optimization structures
 - Lots of optimizations possible: Build hierarchy, Level of Details, Culling Techniques, Impostors,...
- Simulation (Animation, AI, Physics)
- Input event handlers
- Modify data structures
- Database traversal
- Primitive generation
- Shaders (vertex, geometry, fragment)



Graphics Driver

- Command interpretation/translation
 - Host commands → GPU commands
- Handle data transfer
- Memory management
- Emulation of missing features (e.g. full OpenGL 4.5 support)

(2) Geometry Stage

Command

Vertex Processing

Primitive Assembly

Clipping

Perspective Division

Culling

Tesselation

Geometry Shading

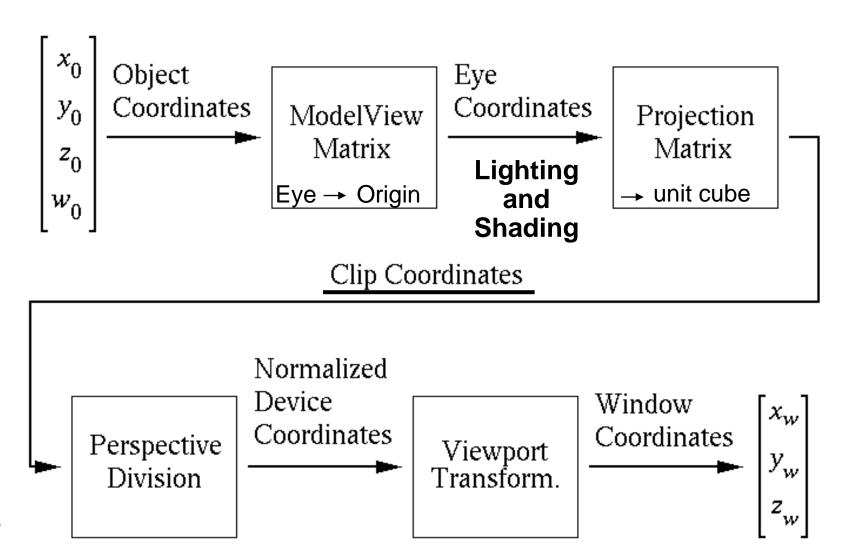


Command

- Command buffering
- Command interpretation
- Unpack and perform format conversion "Input Assembler"

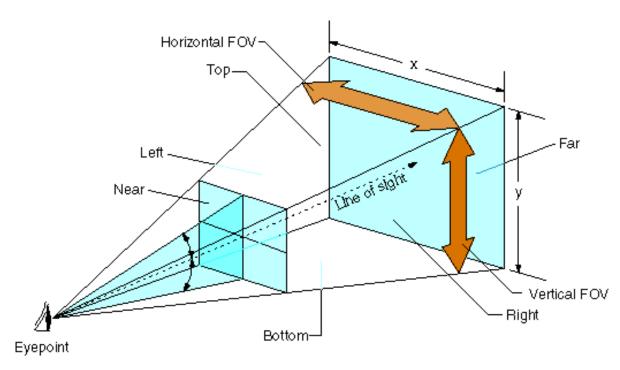


Vertex Processing: Old Geometry Stage





Viewing Frustum



Aspect Ratio =
$$\frac{y}{x}$$
 = $\frac{\tan(\text{vertical FOV/2})}{\tan(\text{horizontal FOV/2})}$



Vertex Processing

- Fixed function pipeline:
 - User has to provide matrices, the rest happens automatically
- Programmable pipeline:
 - User has to provide matrices/other data to shader
 - Shader Code transforms vertex explicitly
 - We can do whatever we want with the vertex!

(3) Rasterization Stage

- Input: 2D Geometric Primitives (Points, Lines, Polys, Bitmaps)
- Primitives needed!
- 1st step output: Fragments (Pixel-Coord. + Color + Depth + Texture-Coord.)
- Polygons are decomposed (various methods)

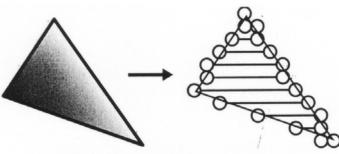
Triangle Setup

Rasterization

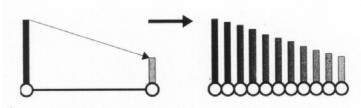
Fragment

Texture Processing Processing

Raster Operations



Polygon decomposition to spans





(3) Rasterization Stage

- Per-Fragment Operations
- Pixel Ownership Test (Window visible?)

Buffers:

- Frame Buffer (Color + Alpha channel)
- Depth Buffer Test (z-Buffer)
- Stencil Buffer
- Accumulation Buffer
- P-Buffer (aux. color buffer -> direct rendering)



Rasterizer/Display Stage

- Framebuffer pixel format: RGBA vs. indexed (colormap)
- Bits: 32, 24 (true color) 16, 15 (high color), 8
- Double buffering, Triple Buffering
- For Stereo: Quad buffer
- Per-window video mode (e.g. stereo, mono)
- Display: frame buffer -> screen



"Modern" Programmable Graphics Pipeline

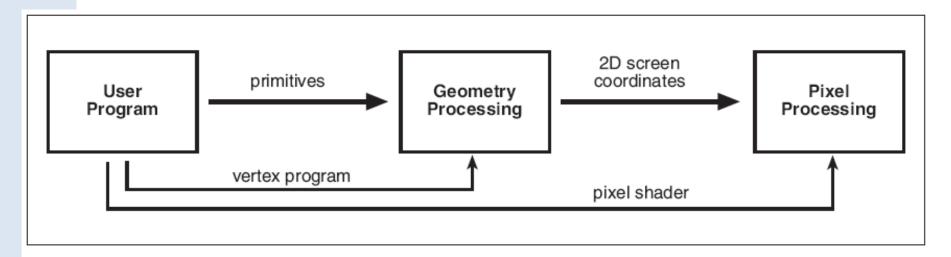


Figure 17.5. The programmable graphics hardware pipeline. The user program supplies primitives, vertex programs, and fragment programs to the hardware.

- Vertex Shader integrated in "old" Geometry Stage
 - Allows per vertex transformations e.g. warping
- Fragment/Pixel Shader integrated in "old" Rasterization Stage
 - Fragment: "pixel" with additional information (alpha, depth, stencil,...)
 - Allows e.g. per pixel lighting,....



Vertex and Fragment Shaders

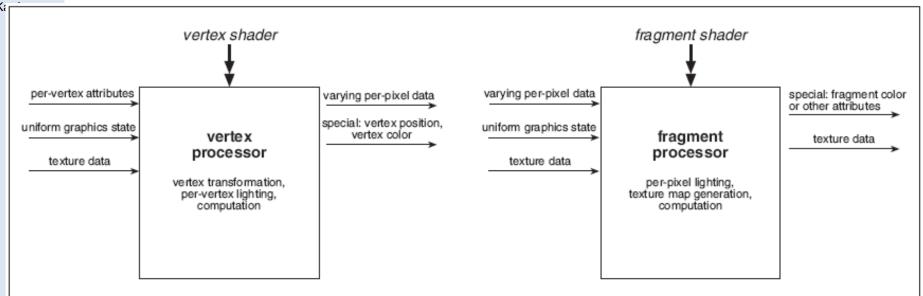
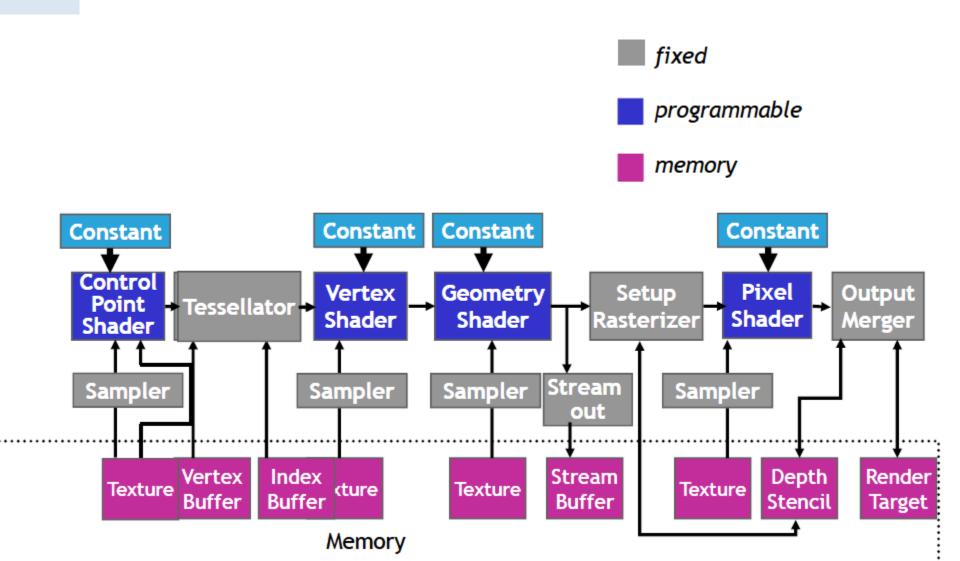


Figure 17.6. The execution model for shader programs. Input, such as per-vertex attributes, graphics state-related uniform variables, varying data, and texture maps are provided to vertex and fragment programs within the shader processor. Shaders output special variables used in later parts of the graphics pipeline.

- Various Shading Languages
 - ARB GPU assembly language (optimized)
 - GLSL (Open GL Shading Language in OpenGL 2.0)
 - HLSL (High Level Shading Language Microsoft)
 - CG (Nvidia) used in Unity



Current OpenGL 4.x / DirectX 11 Architecture





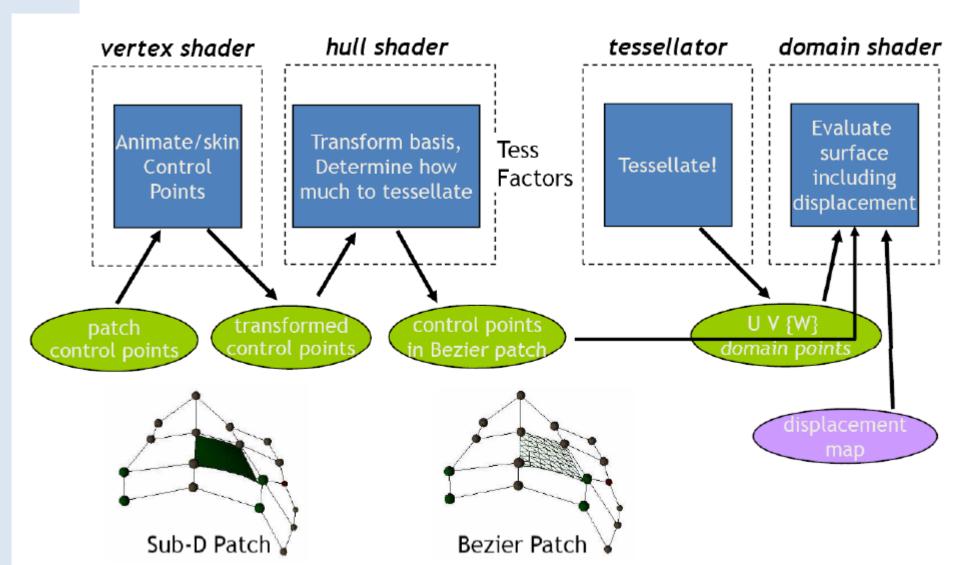
Tesselation



- If just triangles, nothing needs to be done, otherwise:
 - Evaluation of polynomials for curved surfaces
 - Create vertices (tesselation)
- OpenGL 4/ DirectX11 specifies this in hardware
 - 3 new shader stages!
 - Still not trivial (special algorithms required)
- https://www.nvidia.com/content/siggraph/Rollin Oster Open GL CUDA.pdf



DirectX 11 Tesselation

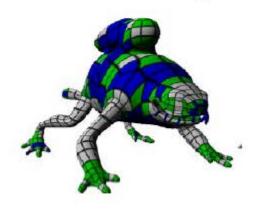


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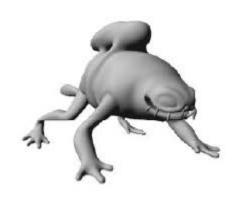


Tesselation Example & Displacement Map

Sub-D Modeling



Animation



Displacement Map



Optimally tesslated!



Mobile Graphics: OpenGL ES

OpenGL ES Momentum

- The leading 3D rendering API for mobile and embedded devices
 - Based on desktop OpenGL but optimized for mobile / handheld devices
 - Removes redundancy & rarely used features adds mobile-friendly data types
 - The power of OpenGL distilled into a much smaller package
- OpenGL ES adopted by every major handset OS
 - Pervasive mobile 3D is evolving fast
- OpenGL ES has become the most widely deployed 3D API
 - Used in diverse applications, devices and markets
 - Mobile phones, games consoles, personal navigation devices, personal media players automotive systems, settop boxes

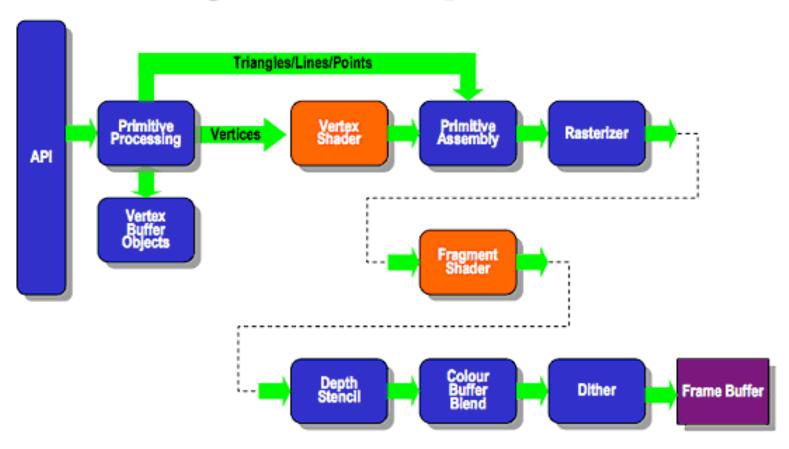






OpenGL ES 2.0

ES2.0 Programmable Pipeline





2014: OpenGL ES 3.x

- 32bit Floating point support
- Texture compression, 3D textures
- Multiple apps can share 3D hardware



Current State

- High bandwidth interconnect of CPU and GPU
 - CPU and streaming units working together
 - Nvidia NVLink
- Heterogeneous architectures
 - CPU and GPU on one chip (especially mobile chips)
 - GPU is treated as a parallel streaming PU
- Whole pipeline is fully programmable (GPU computing)
- Good-bye to the one way graphics pipeline!



Architectural Addition: Real Time Ray Tracing



2018: Nvidia RTX / DirectX Raytracing (DXR)



Star Wars – 1 Quadro RTX 8000



Project Sol – 1 Quadro RTX 6000

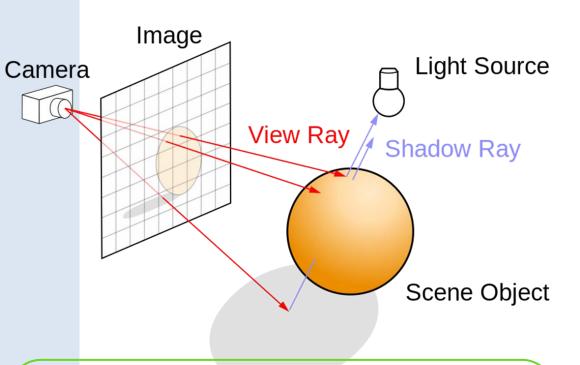


Nvidia Geforce RTX 2080Ti

- 12nm chip (TU102)
- 14.2 TFLOPS single precision math
- 4352 CUDA cores
- 544 Tensor cores
- 68 RT (RayTracing) cores



Ray Tracing Principle



- 1. Construction of the camera/eye rays
- 2. Intersection with the scene objects
- 3. Shading
- 4. Reflection/refraction directions
- 5. Recursion

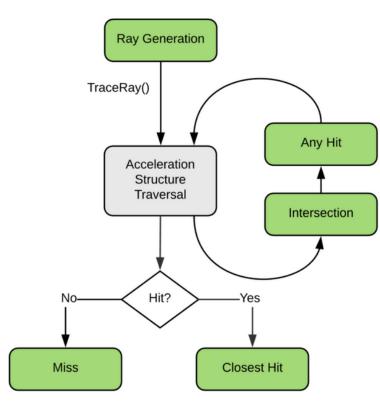
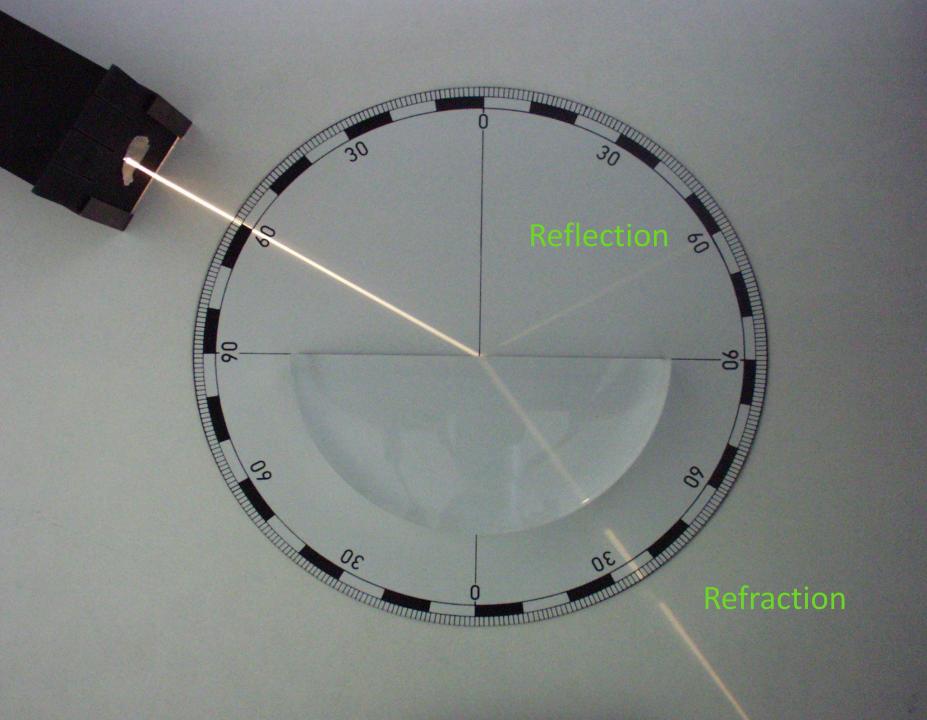


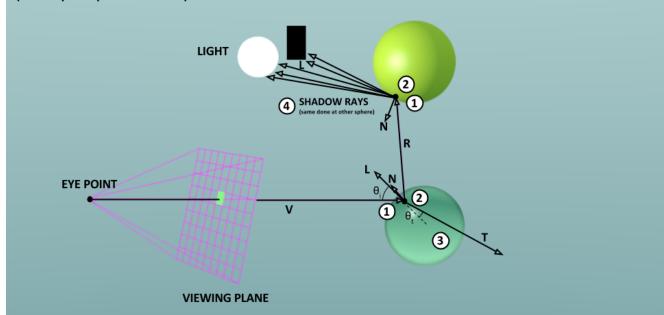
Figure 1. The ray tracing pipeline

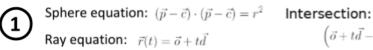




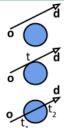
RAY TRACING

(for one pixel up to first bounce)





Ray equation:
$$\vec{r}(t) = \vec{o} + t\vec{d}$$



Illuminiation Equation (Blinn-Phong) with recursive Transmitted and Reflected Intensity:

$$I = k_a I_a + I_i \left(k_d \left(\vec{L} \cdot \vec{N} \right) + k_s \left(\vec{V} \cdot \vec{R} \right)^n \right) + \underbrace{k_t I_t + k_r I_r}_{\text{power in } r}$$

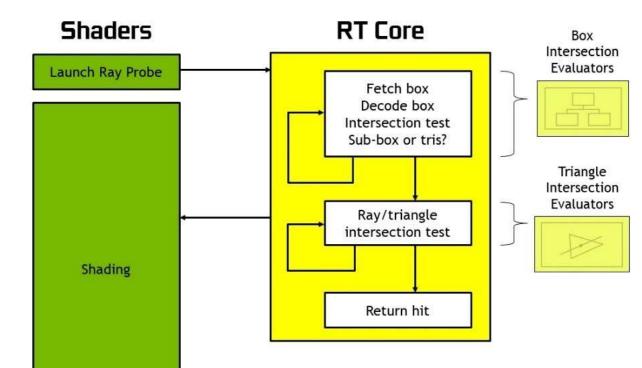
Area Light Simulation: $I_{light} = \frac{\# \text{ (visible shadow rays)}}{\# \text{ (all shadow rays)}}$

BVH ALGORITHM Massive Improvement in Search Efficiency **TORISTICATIONAL PROPERTY OF THE PRO

Nvidia RT cores

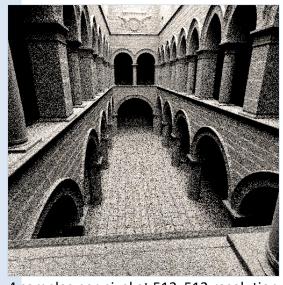
ware Emulation







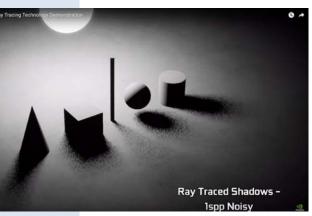
Ray Tracing De-Noising with Deep Learning Networks





4 samples per pixel at 512x512 resolution Our algorithm (Davletaliyev, Kan): 0,48sec

Ground Truth



Nvidia: 1 ray per pixel



Nvidia: 1 ray per pixel – denoised. Real-time!

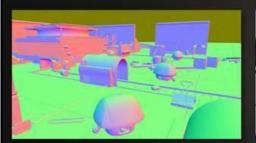


Ground Truth



SEED // PICA PICA: Hardware Raytracing & Turing

Hybrid Rendering Pipeline



Deferred shading (raster)



Direct shadows (raytrace or raster)



Lighting (compute + raytrace)



Reflections (raytrace or compute)



Global Illumination (compute and raytrace)



Ambient occlusion (raytrace or compute)



Transparency & Translucency (raytrace and compute)



Post processing (compute)



Real-time Ray Tracing in AR



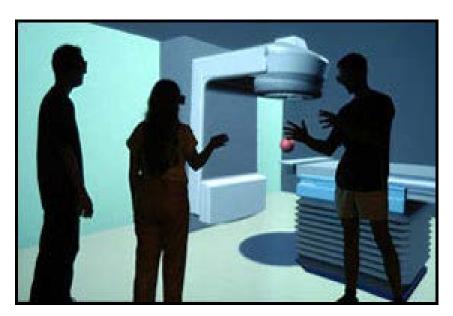
Work by Peter Kan 2012-2014



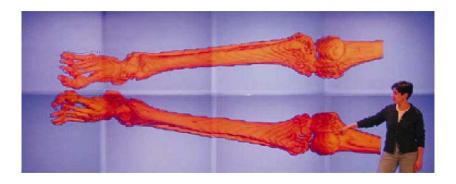
Long term future

- We have...
 - Very high fill rates polygon rates
 - Lots of textures
 - Almost full programmability
 - Few limits (program lengths, memory bandwidth)
 - Real-time ray tracing
- We want (and will get)...
 - Flexible geometry specification
 - Full, easy programmability
 - Higher performance
- Convergence of film rendering and real-time rendering imminent

VR/AR and the Need for Extreme Graphics Power: Examples



Mechanical visualization CAVE, SGI Onyx (8 CPUs, 6 outputs)



Princeton Display Wall 3x8 projectors, 24 PC cluster



HMD setups for larger groups



Parallel Graphics Hardware

Overcome bottleneck by parallel computation

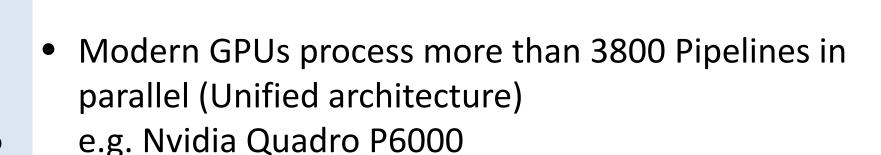
Types of parallel graphics:

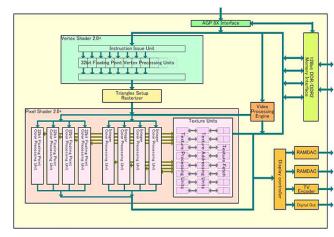
- On-chip / on a graphics board (standard)
- 2. Multiple boards (former: graphics supercomputer) Multiple boards with multi GPUs (1+2)
- 3. PC cluster:
 - Offline Rendering: Standard network Distributed Environment
 - Realtime Rendering: PC cluster with special hardware

Rasterizer

Multiple Graphic Pipelines

- Pipelines fully in HW
- Multiple independent pipelines can be parallelized
- NVIDIA / AMD
 - CUDA cores / streaming processors

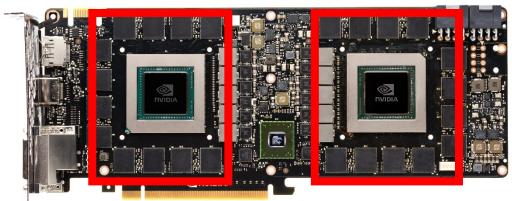




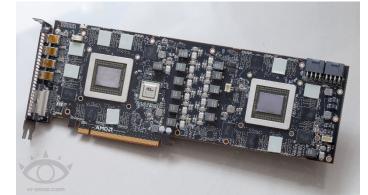
Parallel On-Board

Examples:

- Nvidia Geforce GTX TITAN Z (2014)
 - 2 x 2880 cores



• AMD Radeon R9 295X2 - 2x2816 cores





Parallel Graphics Hardware

Types of parallel graphics:

- 1. On-chip / on a graphics board (standard)
- 2. Multiple boards (former: graphics supercomputer)
 Multiple boards with multi GPUs (1+2)
- 3. PC cluster:
 - Offline Rendering: Standard network Distributed Environment
 - Realtime Rendering: PC cluster with special hardware



Multiple Graphics Boards

Parallel graphics rendering:

- Graphics "Supercomputer"
- PC with SLI or CrossFire

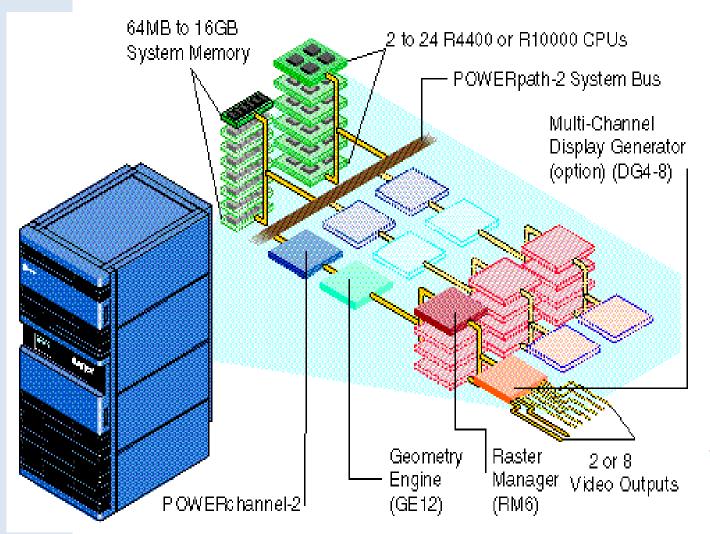
Different:

Multiple display support - (not) synchronized:

- PC with multiple unconnected cards
 - Nvidia Mosaic



Graphics Supercomputer





SGI Onyx with Infinite Reality 3



SGI Onyx 3000 & Infinite Reality 4

G-Brick:

- 4 RasterManager Boards
- 1.3 Gpixel/s/Pipeline
 - (8 subsample/full scene/AA)
- 1 GB Texturspeicher
- 10 GB Framebuffer
- 192 GB/s Bandbreite
- Kombination bis zu 16 IR4





Nvidia Multi-GPU solutions



- Connected via PCle to PC
- 2-8 GPUs
- 12 GB Frame Buffer per GPU
- 2 to 8 Dual-Link Digital Display Connectors
- Genlock/Frame Lock



Supercomputer – Application Areas

- Theme Parks
 (DisneyQuest –
 CyperSpace Mountain)
- Flight Simulators
- Military Applications
- CAVEs / Large setups







Graphics Supercomputer

- Multiple CPUs
- Multiple Geometry Engines
- Multiple Rasterization Engines
- Genlocking
- Multiple Pipes (=graphics cards)
- Multiple Channels (=display outputs)
- Highly configurable
- Now used: standard Nvidia/ATI graphics chips
- On PC: Scalable Link Interface (Nvidia) or CrossFireX (ATI) for PCI Express



Parallel Graphics Hardware

- (A) Computing the same (high resolution) image
- (B) Computing multiple images Multiple outputs



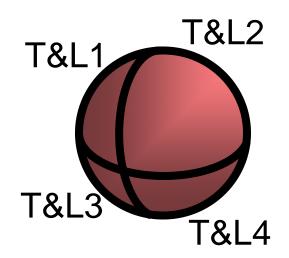
Basic Problems of Parallel Rendering

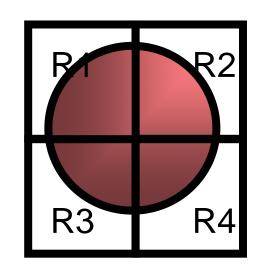
Vertex and Pixel Load Balancing:

- Problem with parallel rendering
 - Load balancing of vertices
 - → 3D (object space) problem
 - Load balancing of pixel (rasterizers)
 - → 2D (screen space) problem

Parallel Rendering as Sorting

- Parallel Geometry Stage
 - Cut 3D model into pieces with equal number of vertices
 - Assign one piece to one T&L unit
- Parallel Rasterization
 - Cut destination image into tiles
 - Assign (triangles contained in) one tile to one rasterizer
- Need to SORT transformed 2D triangles
- Shared common memory





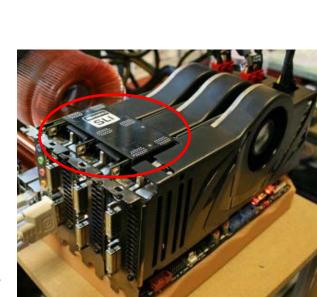


SLI / NVLink (Nvidia)

Scalable Link Interface

3 Modes:

- Split Frame Rendering (SFR) Scissors: Splits each frame and sends half the load to each of the graphics cards
- Alternate Frame Rendering (AFR):
 Frame 1 Card 1, Frame 2 Card 2, alternating
- VR SLI: Right/Left frame computed on Card 1/Card2 in parallel
- PCIe cards are connected by a bridge very fast data transfer
- Optimal performance increase: 1,8 max.

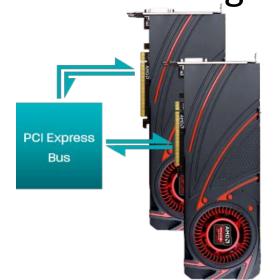


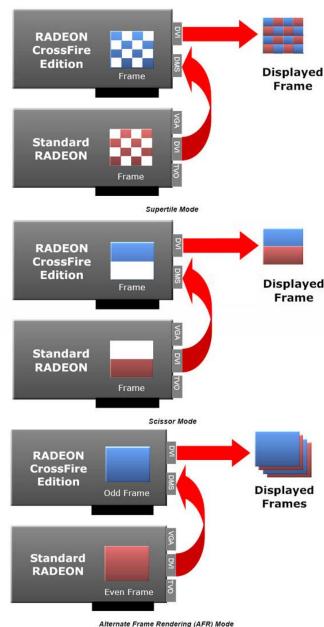


CrossFireX (AMD) / XDMA

3 Modes:

- Supertiling
- Scissors
- Alternate Frame Rendering Additional AA Mode
 No external Bridge needed!







SLI / CrossFire

- Mainboards need to support it
- Connection via separate bridge (PCIe communication) – only for Nvidia.
- AMD used XDMA transfer over PCIe
- CrossFire SuperTiling efficient
- CrossFireX more flexible (supports multiple displays and connection of different AMD cards)
- 2-4 cards can be connected
- VR SLI Mode: Parallel left/right image

Nvidia Mosaic

multiple display configurations with Quadro cards

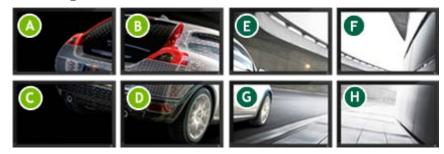




2x3 Configuration



2x4 Configuration



Dual Host Interface Card required to run dual systems.



4-Display Connections for 2-Display Passive





Left Eye





Right Eye



Parallel Graphics Hardware

Types of parallel graphics:

- 1. On-chip / on a graphics board (standard)
- 2. Multiple boards (former: graphics supercomputer) Multiple boards with multi GPUs (1+2)
- 3. PC cluster:
 - Offline Rendering: Standard network Distributed Environment
 - Realtime Rendering: PC cluster with special hardware



Parallel Cluster Rendering (1)

- PC Cluster
 - Off-the-shelf hardware
 - Network (LAN)
 - Cheap
 - Scalable
- Distributed Software
 System





Parallel Cluster Rendering (2)

- power of cluster ≥ power of supercomputer
- Price of cluster << price of supercomputer
- BUT: problems of cluster
 - How to make cluster PCs work together
 - On a single image(or consistent set of images)
- > Parallel Execution of Rendering!
- → Cluster synchronisation (genlocking)!

Cluster Synchronisation

- Q: How to synchronize multiple displays?
- (1) Simple: PC + Multiple graphic outputs
- (2) Not so simple: Multiple workstations





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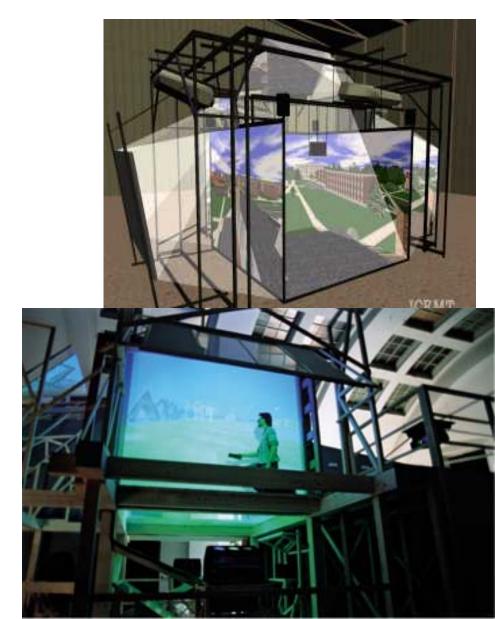
Example:

CAVE

"Computer Assisted Virtual Environment" ™

Has 3 to 6 large screens

- Puts user in a room for visual immersion
- Usually driven by a single or group of powerful graphics engines – nowadays usually PC cluster





Example: CAVE & Shuttering



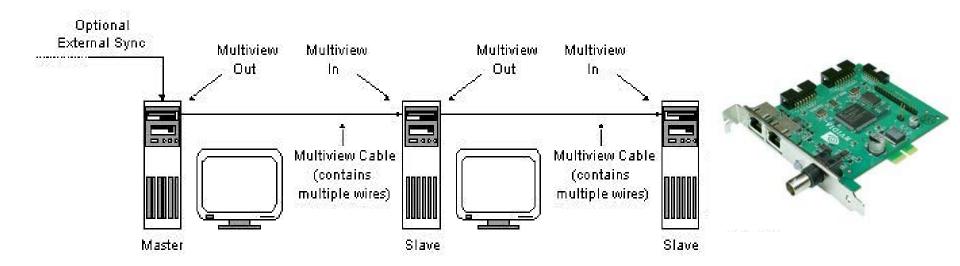
Shutter Glasses





Hardware Synchronisation

Synchronizing multiple displays/workstations



Framelock:

Synchronizing frame buffer swap

Begins redrawing at the same time

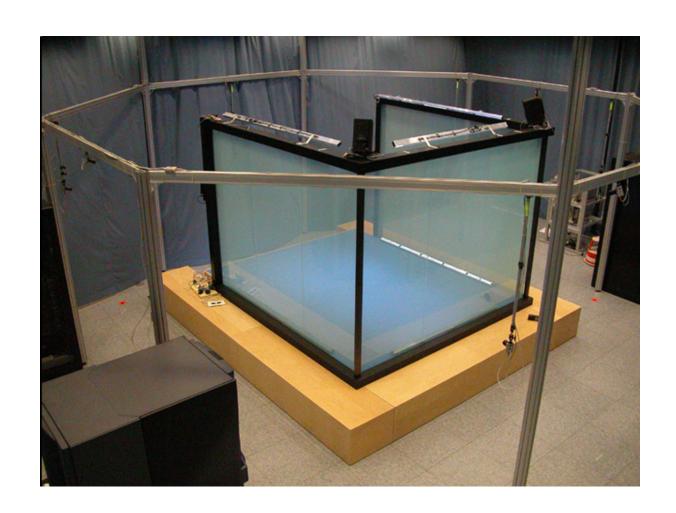
Genlock:

Exact synchronization of vertical synch (electron beam of CRT)

Refreshes each pixel synchronously



Example: Blue-C





3D Card High End Model

- nVidia Quadro RTX 8000 (~ € 10.000.-)
- 48 GB GDDR6 RAM
- Based on Turing Architecture (Geforce RTX 2080)
- 4608 CUDA cores, 576 Tensor cores
- 672 GB/s Bandwidth
- optimized OpenGL drivers (comp. to consumer card)
- 16K x 16K texture resolution
- DX12, Shader Model 6.1,
 OpenGL 4.6, Vulkan 1.1.78





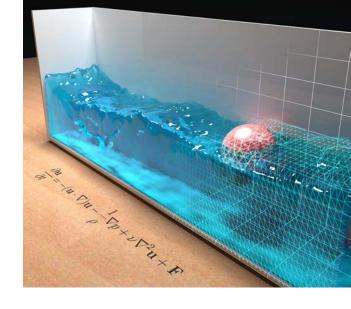
Some Relevant Features (for VR)

- Memory size: 48 GB
- 4 DisplayPorts 1.4 (8K@60Hz or 4K@120Hz), 1
 VirtualLink (1 connector for VR)
- OpenGL quad-buffered stereo (optional 3-pin sync connector); 3D Vision Pro
- NVLink Technology
- Nvidia Mosaic: 2-8 displays
- Fast 3D Texture transfer; HW 3D Window clipping
- Quadro-Sync (optional) with Framelock and Genlock
- HDR technology, 30-bit color, SDI output option
- Quality: 64 x Full-Scene Antialiasing (FSAA), ...



Physics Effects

- Calculation on GPU
- Rigid Bodies, Joints
- Cloth, Particles, Fire, Fluids
- Puts higher rendering load on graphics card
 - SLI recommended







Physics in VR

GRIMAGE Project



Incredible Machine



Microsoft Holodesk



General Purpose Computing

- Nvidia TESLA V100
 - "High Performance Computing" / Deep Learning
 - No graphics card! No graphics output!
 - Programmed using CUDA
 - Additional GPU
 - 5120 CUDA cores
 - 640 Tensor Cores
 - 16 GB HBM2 RAM
 - CUDA C/C++/Fortran, OpenCL,
 DirectCompute Toolkits,



- Alternative: Intel Xeon Phi
 - x86 cores (72 Atom cores)



Nvidia GRID

- GPU Virtualization sharing the GPU
- Low latency remote display
 - "Real time" H.264 encoding
- Grid K2:
 - 2 Kepler GPUs, 3072 cores
 - -8GB RAM





Literatur

- Real-time Rendering
 Tomas Akenine-Möller, Eric Haines, and Naty Hoffman, 1045
 pages, from A.K. Peters Ltd., 3rd edition, ISBN 978-1-56881-424-7, 2008
- http://www.realtimerendering.com/